

# **Tutorial Problems: Nuclear Physics**

## **PH:504**

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1. The radius  $R$  of a nucleus with mass number  $A$  is given by the formula  $R = r_0 A^{1/3}$  with  $r_0 \simeq 1.2 \text{ fm}$ . Using the Fermi-gas model show that the energy  $E_F$  of the Fermi level in a nucleus with equal numbers of protons and neutrons is given by :  $E_F = \frac{\hbar^2}{2M_p r_0^2} \left(\frac{9\pi}{8}\right)^{2/3}$ . Hence, estimate the total kinetic energy of the nucleons the nucleus  $^{16}\text{O}$ . [Marks : 5]
  2. By considering the conservation of energy and momentum show that a free electron cannot absorb a photon. Why can absorption occur if the electron is initially bound ? [Marks : 3]
  3. The principal source of energy produced in the Sun is nuclear fusion via the pp chain :
    - (a)  $p + p \rightarrow p + {}_1^2\text{H} + e^+ + \nu + 0.42 \text{ MeV}$
    - (b)  $p + {}_1^2\text{H} \rightarrow {}_2^3\text{He} + \gamma + \nu + 5.49 \text{ MeV}$
    - (c)  ${}_2^3\text{He} + {}_2^3\text{He} \rightarrow {}_2^4\text{He} + p + p + 12.86 \text{ MeV}$

On average the neutrinos each take away 0.26 MeV. The flux of radiant energy at the distance of the Earth from the Sun is  $1.37 \text{ kW m}^{-2}$ . Calculate the flux of solar neutrinos at the Earth. [Marks : 5]
  4. A beam of 1.5 MeV neutrons, of intensity  $I_0 = 5 \times 10^{14} \text{ cm}^{-2} \text{ s}^{-1}$  is incident on a slab of copper of thickness  $d = 0.75 \text{ cm}$ . The emergent beam has intensity  $I = 0.23 I_0$ . Calculate the total cross-section of neutrons on copper at this energy. [Hints :  $\sigma = \frac{\mu}{n_t}$ ,  $n_t = \rho N_A / A$ , density of copper,  $\rho_{Cu} = 8.96 \text{ g cm}^{-3}$ , atomic weight of natural copper,  $A = 63.5$ .] [5 Marks][Ref : Lilley, Nuclear Physics]
  5. In the decay of  $^{64}\text{Cu}$  both neutrinos and antineutrinos are observed.
    - a) What are the two possible beta-decay processes and products? b) Calculate the Q values for both decay modes. [Marks : 1+4=5]
  6. Give a brief description of the reactions involved in the primordial nucleosynthesis. List the nuclides that play major roles in the primordial nucleosynthesis. [5+2 Marks]
  7. What are the major challenges in the computation of reaction rates involved in primordial nucleosynthesis? What do you mean by Astrophysical S-factor. How can you connect it to the probability of tunneling through the mutual Coulomb barrier of interacting nuclei? Hence indicate the importance of S-factor in the computation of Nuclear reaction rate. [Ref : Nuclear Astrophysics- A Course of Lectures; Journal Ref : Nuclear Physics A, Volume 986, June 2019, Pages 98-106] [3+2+3+2 Marks]
  8. Discuss the role of nuclear fusion reactions in the energy production in the stars. Give an account of the major reactions involved in the CNO-cycle. [5+3 Marks]
  9. What do you mean by r- and s-processes? How the heavy elements (elements beyond iron) are produced in the stars. Explain with suitable block diagram [2+4 Marks]

10. What are the main components of a nuclear reactor? Discuss the role of moderators in the reactors. What are the main criterion for sustained operation of a nuclear reactor? [2+2+1 marks]
11. With suitable example explain the origin of odd-parity levels in addition to the  $0+$ ,  $2+$ ,  $4+$ , etc levels in the energy spectrum of even-even nuclei. [Hints : Class work] [3 Marks]
12. Explain why quadrupole mode of oscillation is considered most important in the collective model of nuclei. State the conditions under which prolate and oblate shape of deformed nuclei are observed. [2+2 Marks]
13. Define Clebsch-Gordon coefficient. What are the symmetry rules obeyed by these coefficients? List all the CGC's appearing in the expression for  $|J=1, M=1\rangle$  for two fermionic system with  $j_1 = 1/2, j_2 = 3/2$ . [5 Marks]

by Dr M A Khan